1 Adding Fractions

1.1 Exercises

Exercise 1 – Solution

1. Goal?

We want to add the fractions $\frac{1}{2}$ and $\frac{1}{3}$.

2. Simplify?

Neither $\frac{1}{2}$ nor $\frac{1}{3}$ can be simplified.

3. Least Common Denominator

$$\frac{1}{2} = \frac{1 \times 3}{2 \times 3} = \frac{3}{6} \; ; \quad \frac{1}{3} = \frac{1 \times 2}{3 \times 2} = \frac{2}{6}$$
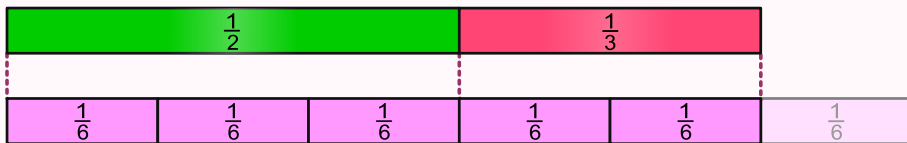
4. Add

$$\frac{3}{6} + \frac{2}{6} = \frac{5}{6}$$

5. Simplify?

$\frac{5}{6}$ cannot be simplified.

6. Result

$$\frac{1}{2} + \frac{1}{3} = \frac{1 \times 3}{2 \times 3} + \frac{1 \times 2}{3 \times 2} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6}$$

Exercise 1 – Level 1

1. Goal?

$$\frac{1}{2} + \frac{1}{3}$$

2. Simplify?

$$\frac{1}{2} =$$

$$\frac{1}{3} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$\frac{1}{2}$ $\frac{1}{3}$

Exercise 1 – Level 2

1. Goal?

$$\frac{1}{2} + \frac{1}{3}$$

2. Simplify?

$$\frac{1}{2} =$$ $$\frac{1}{3} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 1 – Level 3

1. Goal?

$$\frac{1}{2} + \frac{1}{3}$$

2. Simplify?

$\frac{1}{2} =$ $\frac{1}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 2 – Solution

1. Goal?

We want to add the fractions $\frac{1}{6}$ and $\frac{1}{2}$.

2. Simplify?

Neither $\frac{1}{6}$ nor $\frac{1}{2}$ can be simplified.

3. Least Common Denominator

$$\frac{1}{6} \;\; ; \;\; \frac{1}{2} = \frac{1 \times 3}{2 \times 3} = \frac{3}{6}$$

4. Add

$$\frac{1}{6} + \frac{3}{6} = \frac{4}{6}$$

5. Simplify?

$$\frac{4}{6} = \frac{4 \div 2}{6 \div 2} = \frac{2}{3}$$

6. Result

$$\frac{1}{6} + \frac{1}{2} = \frac{1}{6} + \frac{1 \times 3}{2 \times 3} = \frac{1}{6} + \frac{3}{6} = \frac{4}{6} = \frac{4 \div 2}{6 \div 2} = \frac{2}{3}$$

Exercise 2 – Level 1

1. Goal?

$$\frac{1}{6} + \frac{1}{2}$$

2. Simplify?

$\frac{1}{6} =$ $\frac{1}{2} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 2 – Level 2

1. Goal?

$$\frac{1}{6} + \frac{1}{2}$$

2. Simplify?

$\frac{1}{6} =$ $\qquad\qquad\qquad$ $\frac{1}{2} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$\frac{1}{2}$	$\frac{1}{6}$

Exercise 2 – Level 3

1. Goal?

$$\frac{1}{6} + \frac{1}{2}$$

2. Simplify?

$\frac{1}{6} =$ $\frac{1}{2} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 3 – Solution

1. Goal?

We want to add the fractions $\frac{1}{2}$ and $\frac{3}{10}$.

2. Simplify?

Neither $\frac{1}{2}$ nor $\frac{3}{10}$ can be simplified.

3. Least Common Denominator

$$\frac{1}{2} = \frac{1 \times 5}{2 \times 5} = \frac{5}{10} \ ; \ \frac{3}{10}$$

4. Add

$$\frac{5}{10} + \frac{3}{10} = \frac{8}{10}$$

5. Simplify?

$$\frac{8}{10} = \frac{8 \div 2}{10 \div 5} = \frac{4}{5}$$

6. Result

$$\frac{1}{2} + \frac{3}{10} = \frac{1 \times 5}{2 \times 5} + \frac{3}{10} = \frac{5}{10} + \frac{3}{10} = \frac{8}{10} = \frac{8 \div 2}{10 \div 2} = \frac{4}{10}$$

Exercise 3 – Level 1

1. Goal?

$$\frac{1}{2} + \frac{3}{10}$$

2. Simplify?

$\frac{1}{2} =$ $\frac{3}{10} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 3 – Level 2

1. Goal?

$$\frac{1}{2} + \frac{3}{10}$$

2. Simplify?

$\frac{1}{2} =$ $\frac{3}{10} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 3 – Level 3

1. Goal?

$$\frac{1}{2} + \frac{3}{10}$$

2. Simplify?

$$\frac{1}{2} =$$

$$\frac{3}{10} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 4 – Solution

1. Goal?

We want to add the fractions $\frac{1}{4}$ and $\frac{1}{3}$.

2. Simplify?

Neither $\frac{1}{4}$ nor $\frac{1}{3}$ can be simplified.

3. Least Common Denominator

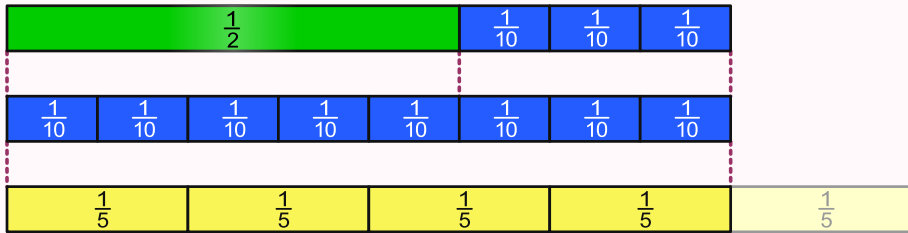$$\frac{1}{4} = \frac{1 \times 3}{4 \times 3} = \frac{3}{12} \;;\; \frac{1}{3} = \frac{1 \times 4}{3 \times 4} = \frac{4}{12}$$

4. Add

$$\frac{4}{12} + \frac{3}{12} = \frac{7}{12}$$

5. Simplify?

$\frac{7}{12}$ cannot be simplified.

6. Result

$$\frac{1}{4} + \frac{1}{3} = \frac{1 \times 3}{4 \times 3} + \frac{1 \times 4}{3 \times 4} = \frac{3}{12} + \frac{4}{12} = \frac{7}{12}$$

Exercise 4 – Level 1

1. Goal?

$$\frac{1}{4} + \frac{1}{3}$$

2. Simplify?

$$\frac{1}{4} =$$
$$\frac{1}{3} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 4 – Level 2

1. Goal?

$$\frac{1}{4} + \frac{1}{3}$$

2. Simplify?

$\frac{1}{4} =$ $\frac{1}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 4 – Level 3

1. Goal?

$$\frac{1}{4} + \frac{1}{3}$$

2. Simplify?

$\frac{1}{4} =$ $\frac{1}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 5 – Solution

1. Goal?

We want to add the fractions $\frac{2}{3}$ and $\frac{1}{5}$.

2. Simplify?

Neither $\frac{2}{3}$ nor $\frac{1}{5}$ can be simplified.

3. Least Common Denominator

$$\frac{2}{3} = \frac{2 \times 5}{3 \times 5} = \frac{10}{15} \;;\;\; \frac{1}{5} = \frac{1 \times 3}{5 \times 3} = \frac{3}{15}$$
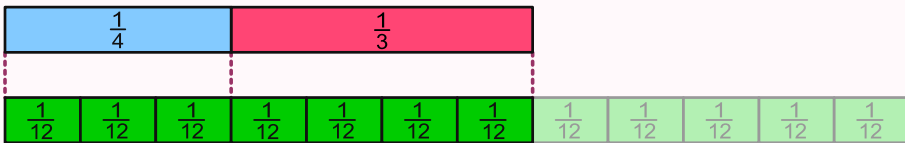
4. Add

$$\frac{10}{15} + \frac{3}{15} = \frac{13}{15}$$

5. Simplify?

$\frac{13}{15}$ cannot be simplified.

6. Result

$$\frac{2}{3} + \frac{1}{5} = \frac{2 \times 5}{3 \times 5} + \frac{1 \times 3}{5 \times 3} = \frac{10}{15} + \frac{3}{15} = \frac{13}{15}$$

$\frac{1}{3}$					$\frac{1}{3}$					$\frac{1}{5}$		

$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$	$\frac{1}{15}$

Exercise 5 – Level 1

1. Goal?

$$\frac{2}{3} + \frac{1}{5}$$

2. Simplify?

$\frac{2}{3} =$ $\frac{1}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{3}$ | $\frac{1}{3}$ | $\frac{1}{5}$ |

Exercise 5 – Level 2

1. Goal?

$$\frac{2}{3} + \frac{1}{5}$$

2. Simplify?

$\frac{2}{3} =$ $\frac{1}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 5 – Level 3

1. Goal?

$$\frac{2}{3} + \frac{1}{5}$$

2. Simplify?

$$\frac{2}{3} =$$
$$\frac{1}{5} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 6 – Solution

1. Goal?

We want to add the fractions $\frac{2}{4}$ and $\frac{2}{6}$.

2. Simplify?

$$\frac{2}{4} = \frac{2 \div 2}{4 \div 2} = \frac{1}{2} \quad ; \quad \frac{2}{6} = \frac{2 \div 2}{6 \div 2} = \frac{1}{3}$$

3. Least Common Denominator

$$\frac{1}{2} = \frac{1 \times 3}{2 \times 3} = \frac{3}{6} \; ; \; \frac{1}{3} = \frac{1 \times 2}{3 \times 2} = \frac{2}{6}$$
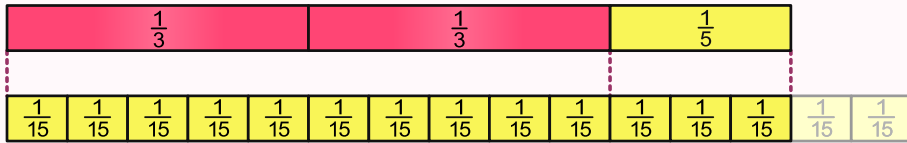
4. Add

$$\frac{3}{6} + \frac{2}{6} = \frac{5}{6}$$

5. Simplify?

$\frac{5}{6}$ cannot be simplified.

6. Result

$$\frac{2}{4} + \frac{2}{6} = \frac{2 \div 2}{4 \div 2} + \frac{2 \div 2}{6 \div 2} = \frac{1}{2} + \frac{1}{3} = \frac{1 \times 3}{2 \times 3} + \frac{1 \times 2}{2 \times 3} = \frac{3}{6} + \frac{2}{6} = \frac{5}{6}$$

| $\frac{1}{4}$ | $\frac{1}{4}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

| $\frac{1}{2}$ | $\frac{1}{3}$ |

| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

Exercise 6 – Level 1

1. Goal?

$$\frac{2}{4} + \frac{2}{6}$$

2. Simplify?

$\frac{2}{4} =$ $\frac{2}{6} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$\frac{1}{4}$	$\frac{1}{4}$	$\frac{1}{6}$	$\frac{1}{6}$

Exercise 6 – Level 2

1. Goal?

$$\frac{2}{4} + \frac{2}{6}$$

2. Simplify?

$\frac{2}{4} =$ $\frac{2}{6} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 6 – Level 3

1. Goal?

$$\frac{2}{4} + \frac{2}{6}$$

2. Simplify?

$\frac{2}{4} =$ $\frac{2}{6} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 7 – Solution

1. Goal?

We want to add the fractions $\frac{3}{10}$ and $\frac{1}{5}$.

2. Simplify?

Neither $\frac{3}{10}$ nor $\frac{1}{5}$ can be simplified.

3. Least Common Denominator

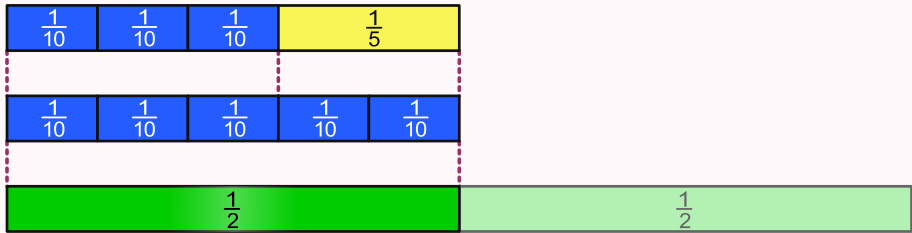$$\frac{3}{10} \ ; \ \frac{1}{5} = \frac{1 \times 2}{5 \times 2} = \frac{2}{10}$$

4. Add

$$\frac{3}{10} + \frac{2}{10} = \frac{5}{10}$$

5. Simplify?

$$\frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$

6. Result

$$\frac{3}{10} + \frac{1}{5} = \frac{3}{10} + \frac{1 \times 2}{5 \times 2} = \frac{3}{10} + \frac{2}{10} = \frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$

$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{5}$

$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$	$\frac{1}{10}$

$\frac{1}{2}$	$\frac{1}{2}$

Exercise 7 – Level 1

1. Goal?

$$\frac{3}{10} + \frac{1}{5}$$

2. Simplify?

$\frac{3}{10} =$ $\frac{1}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 7 – Level 2

1. Goal?

$$\frac{3}{10} + \frac{1}{5}$$

2. Simplify?

$\frac{3}{10} =$ $\frac{1}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 7 – Level 3

1. Goal?

$$\frac{3}{10} + \frac{1}{5}$$

2. Simplify?

$\frac{3}{10} =$ $\frac{1}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 8 – Solution

1. Goal?

We want to add the fractions $\frac{3}{4}$ and $\frac{2}{5}$.

2. Simplify?

Neither $\frac{3}{4}$ nor $\frac{2}{5}$ can be simplified.

3. Least Common Denominator

$$\frac{3}{4} = \frac{3 \times 5}{4 \times 5} = \frac{15}{20} \; ; \quad \frac{2}{5} = \frac{2 \times 4}{5 \times 4} = \frac{8}{20}$$

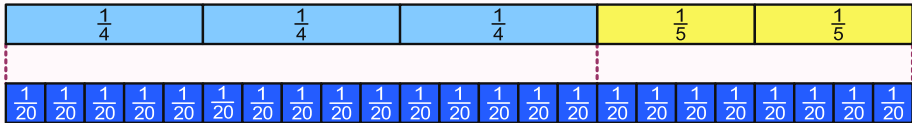**4. Add**

$$\frac{15}{20} + \frac{8}{20} = \frac{23}{20}$$

5. Simplify?

$\frac{23}{20}$ cannot be simplified.

6. Result

$$\frac{3}{4} + \frac{2}{5} = \frac{3 \times 5}{4 \times 5} + \frac{2 \times 4}{5 \times 2} = \frac{15}{20} + \frac{8}{20} = \frac{23}{20}$$
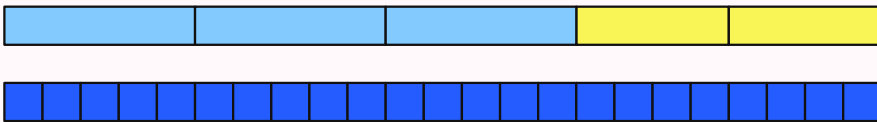
Exercise 8 – Level 1

1. Goal?

$$\frac{3}{4} + \frac{2}{5}$$

2. Simplify?

$$\frac{3}{4} =$$

$$\frac{2}{5} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 8 – Level 2

1. Goal?

$$\frac{3}{4} + \frac{2}{5}$$

2. Simplify?

$\frac{3}{4} =$ $\frac{2}{5} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 8 – Level 3

1. Goal?

$$\frac{3}{4} + \frac{2}{5}$$

2. Simplify?

$$\frac{3}{4} =$$
$$\frac{2}{5} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 9 – Solution

1. Goal?

We want to add the fractions $\frac{6}{20}$ and $\frac{9}{18}$.

2. Simplify?

$$\frac{6}{20} = \frac{6 \div 2}{20 \div 2} = \frac{3}{10} \qquad \frac{9}{18} = \frac{9 \div 9}{18 \div 9} = \frac{1}{2}$$

3. Least Common Denominator

$$\frac{3}{10} \; ; \; \frac{1}{2} = \frac{1 \times 5}{2 \times 5} = \frac{5}{10}$$

4. Add

$$\frac{3}{10} + \frac{5}{10} = \frac{8}{10}$$

5. Simplify?

$$\frac{8}{10} = \frac{8 \div 2}{10 \div 2} = \frac{4}{5}$$

6. Result

$$\frac{6}{20}+\frac{9}{18} = \frac{6 \div 2}{20 \div 2}+\frac{9 \div 9}{18 \div 9} = \frac{3}{10}+\frac{1}{2} = \frac{3}{10}+\frac{1 \times 5}{2 \times 5} = \frac{3}{10}+\frac{5}{10} = \frac{8}{10} = \frac{8 \div 2}{10 \div 2} = \frac{4}{5}$$

Exercise 9 – Level 1

1. Goal?

$$\frac{6}{20} + \frac{9}{18}$$

2. Simplify?

$$\frac{6}{20} =$$

$$\frac{9}{18} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ |

Exercise 9 – Level 2

1. Goal?

$$\frac{6}{20} + \frac{9}{18}$$

2. Simplify?

$$\frac{6}{20} = \qquad\qquad \frac{9}{18} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ |

Exercise 9 – Level 3

1. Goal?

$$\frac{6}{20} + \frac{9}{18}$$

2. Simplify?

$$\frac{6}{20} =$$ $$\frac{9}{18} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 10 – Solution

1. Goal?

We want to add the fractions $\frac{4}{8}$ and $\frac{5}{30}$.

2. Simplify?

$$\frac{4}{8} = \frac{4 \div 4}{8 \div 4} = \frac{1}{2} \quad ; \quad \frac{5}{30} = \frac{5 \div 5}{30 \div 5} = \frac{1}{6}$$

3. Least Common Denominator

$$\frac{1}{2} = \frac{1 \times 3}{2 \times 3} = \frac{3}{6} \; ; \; \frac{1}{6}$$

4. Add

$$\frac{3}{6} + \frac{1}{6} = \frac{4}{6}$$

5. Simplify?

$$\frac{4}{6} = \frac{4 \div 2}{6 \div 2} = \frac{2}{3}$$

6. Result

$$\frac{4}{8} + \frac{5}{30} = \frac{4 \div 4}{8 \div 4} + \frac{5 \div 5}{30 \div 5} = \frac{1}{2} + \frac{1}{6} = \frac{1 \times 3}{2 \times 3} + \frac{1}{6} = \frac{3}{6} + \frac{1}{6} = \frac{4}{6} = \frac{4 \div 2}{6 \div 2} = \frac{2}{3}$$

Exercise 10 – Level 1

1. Goal?

$$\frac{4}{8} + \frac{5}{30}$$

2. Simplify?

$$\frac{4}{8} =$$

$$\frac{5}{30} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 10 – Level 2

1. Goal?

$$\frac{4}{8} + \frac{5}{30}$$

2. Simplify?

$$\frac{4}{8} =$$

$$\frac{5}{30} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{8}$ | $\frac{1}{30}$ $\frac{1}{30}$ $\frac{1}{30}$ $\frac{1}{30}$ $\frac{1}{30}$ |

Exercise 10 – Level 3

1. Goal?
$$\frac{4}{8} + \frac{5}{30}$$

2. Simplify?

$\frac{4}{8} =$ $\frac{5}{30} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 11 – Solution

1. Goal?

We want to add the fractions $\frac{1}{4}$ and $\frac{5}{12}$.

2. Simplify?

Neither $\frac{1}{4}$ nor $\frac{5}{12}$ can be simplified.

3. Least Common Denominator

$$\frac{1}{4} = \frac{1 \times 3}{4 \times 3} = \frac{3}{12} \quad ; \quad \frac{5}{12}$$

4. Add

$$\frac{3}{12} + \frac{5}{12} = \frac{8}{12}$$

5. Simplify?

$$\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

6. Result

$$\frac{1}{4} + \frac{5}{12} = \frac{1 \times 3}{4 \times 3} + \frac{5}{12} = \frac{3}{12} + \frac{5}{12} = \frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

Exercise 11 – Level 1

1. Goal?

$$\frac{1}{4} + \frac{5}{12}$$

2. Simplify?

$\frac{1}{4} =$ $\qquad\qquad\qquad\qquad$ $\frac{5}{12} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 11 – Level 2

1. Goal?

$$\frac{1}{4} + \frac{5}{12}$$

2. Simplify?

$$\frac{1}{4} = \qquad\qquad\qquad \frac{5}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 11 – Level 3

1. Goal?

$$\frac{1}{4} + \frac{5}{12}$$

2. Simplify?

$\frac{1}{4} =$ $\frac{5}{12} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 12 – Solution

1. Goal?

We want to add the fractions $\frac{7}{15}$ and $\frac{1}{3}$.

2. Simplify?

Neither $\frac{7}{15}$ nor $\frac{1}{3}$ can be simplified.

3. Least Common Denominator

$$\frac{7}{15} \ ; \ \frac{1}{3} = \frac{1 \times 5}{3 \times 5} = \frac{5}{15}$$

4. Add

$$\frac{7}{15} + \frac{5}{15} = \frac{12}{15}$$

5. Simplify?

$$\frac{12}{15} = \frac{12 \div 3}{15 \div 3} = \frac{4}{5}$$

6. Result

$$\frac{7}{15} + \frac{1}{3} = \frac{7}{15} + \frac{1 \times 5}{3 \times 5} = \frac{7}{15} + \frac{5}{15} = \frac{12}{15} = \frac{12 \div 3}{15 \div 3} = \frac{4}{5}$$

| $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{3}$ |

| $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ | $\frac{1}{15}$ |

| $\frac{1}{5}$ | $\frac{1}{5}$ | $\frac{1}{5}$ | $\frac{1}{5}$ | $\frac{1}{5}$ |

Exercise 12 – Level 1

1. Goal?

$$\frac{7}{15} + \frac{1}{3}$$

2. Simplify?

$$\frac{7}{15} =$$

$$\frac{1}{3} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 12 – Level 2

1. Goal?

$$\frac{7}{15} + \frac{1}{3}$$

2. Simplify?

$$\frac{7}{15} =$$

$$\frac{1}{3} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

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Exercise 12 – Level 3

1. Goal?
$$\frac{7}{15} + \frac{1}{3}$$

2. Simplify?

$\frac{7}{15} =$ $\frac{1}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 13 – Solution

1. Goal?

We want to add the fractions $\frac{5}{18}$ and $\frac{5}{6}$.

2. Simplify?

Neither $\frac{5}{18}$ nor $\frac{5}{6}$ can be simplified.

3. Least Common Denominator

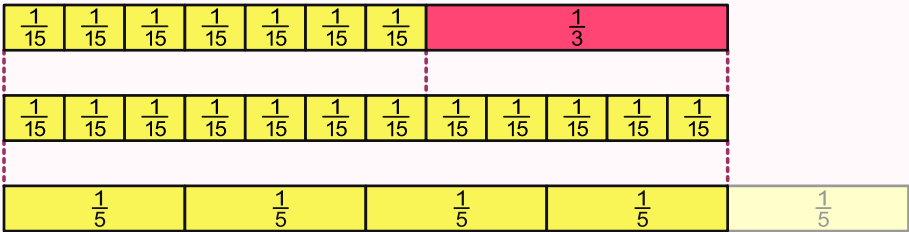$$\frac{5}{18} \; ; \; \frac{5}{6} = \frac{5 \times 3}{6 \times 3} = \frac{15}{18}$$

4. Add

$$\frac{5}{18} + \frac{15}{18} = \frac{20}{18}$$

5. Simplify?

$$\frac{20}{18} = \frac{20 \div 2}{18 \div 2} = \frac{10}{9}$$

6. Result

$$\frac{5}{18} + \frac{5}{6} = \frac{5}{18} + \frac{5 \times 3}{6 \times 3} = \frac{5}{18} + \frac{15}{18} = \frac{20}{18} = \frac{20 \div 2}{18 \div 2} = \frac{10}{9}$$

| $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

| $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ |

| $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ | $\frac{1}{9}$ |

Exercise 13 – Level 1

1. Goal?

$$\frac{5}{18} + \frac{5}{6}$$

2. Simplify?

$$\frac{5}{18} =$$

$$\frac{5}{6} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

Exercise 13 – Level 2

---

1. Goal?

$$\frac{5}{18} + \frac{5}{6}$$

---

2. Simplify?

$$\frac{5}{18} =$$
$$\frac{5}{6} =$$

---

3. Least Common Denominator

---

4. Add

---

5. Simplify?

---

6. Result

| $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{18}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

Exercise 13 – Level 3

1. Goal?

$$\frac{5}{18} + \frac{5}{6}$$

2. Simplify?

$\frac{5}{18} =$ $\qquad\qquad\qquad\qquad$ $\frac{5}{6} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 14 – Solution

1. Goal?

We want to add the fractions $\frac{4}{14}$ and $\frac{2}{3}$.

2. Simplify?

$$\frac{4}{14} = \frac{4 \div 2}{14 \div 2} = \frac{2}{7} \quad ; \quad \frac{2}{3}$$

3. Least Common Denominator

$$\frac{2}{7} = \frac{2 \times 3}{7 \times 3} = \frac{6}{21} \ ; \ \frac{2}{3} = \frac{2 \times 7}{3 \times 7} = \frac{14}{21}$$

4. Add

$$\frac{6}{21} + \frac{14}{21} = \frac{20}{21}$$

5. Simplify?

$\frac{20}{21}$ cannot be simplified.

6. Result

$$\frac{4}{14} + \frac{2}{3} = \frac{4 \div 2}{14 \div 2} + \frac{2}{3} = \frac{2}{7} + \frac{2}{3} = \frac{2 \times 3}{7 \times 3} + \frac{2 \times 7}{3 \times 7} = \frac{6}{21} + \frac{14}{21} = \frac{20}{21}$$

$\frac{1}{14}$	$\frac{1}{14}$	$\frac{1}{14}$	$\frac{1}{14}$	$\frac{1}{3}$	$\frac{1}{3}$

$\frac{1}{7}$	$\frac{1}{7}$	$\frac{1}{3}$	$\frac{1}{3}$

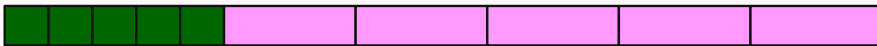| $\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$	$\frac{1}{21}$

Exercise 14 – Level 1

1. Goal?

$$\frac{4}{14} + \frac{2}{3}$$

2. Simplify?

$\frac{4}{14} =$ $\frac{2}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 14 – Level 2

1. Goal?
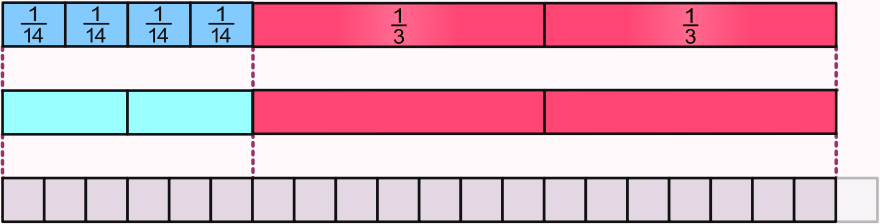$$\frac{4}{14} + \frac{2}{3}$$

2. Simplify?

$\frac{4}{14} =$ $\qquad\qquad\qquad$ $\frac{2}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{14}$ | $\frac{1}{14}$ | $\frac{1}{14}$ | $\frac{1}{14}$ | $\frac{1}{3}$ | $\frac{1}{3}$ |

Exercise 14 – Level 3

1. Goal?

$$\frac{4}{14} + \frac{2}{3}$$

2. Simplify?

$\frac{4}{14} =$
 $\frac{2}{3} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 15 – Solution

1. Goal?

We want to add the fractions $\frac{3}{9}$ and $\frac{5}{30}$.

2. Simplify?

$$\frac{3}{9} = \frac{3 \div 3}{9 \div 3} = \frac{1}{3} \qquad ; \qquad \frac{5}{30} = \frac{5 \div 5}{30 \div 5} = \frac{1}{6}$$

3. Least Common Denominator

$$\frac{1}{3} = \frac{1 \times 2}{3 \times 2} = \frac{2}{6} \ ; \ \frac{1}{6}$$

4. Add

$$\frac{2}{6} + \frac{1}{6} = \frac{3}{6}$$

5. Simplify?

$$\frac{3}{6} = \frac{3 \div 3}{6 \div 3} = \frac{1}{2}$$

6. Result

$$\frac{3}{9} + \frac{5}{30} = \frac{3 \div 3}{9 \div 3} + \frac{5 \div 5}{30 \div 5} = \frac{1}{3} + \frac{1}{6} = \frac{1 \times 2}{3 \times 2} + \frac{1}{6} = \frac{2}{6} + \frac{1}{6} = \frac{3}{6} = \frac{3 \div 2}{6 \div 2} = \frac{1}{2}$$

Exercise 15 – Level 1

1. Goal?

$$\frac{3}{9} + \frac{5}{30}$$

2. Simplify?

$$\frac{3}{9} =$$
$$\frac{5}{30} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 15 – Level 2

1. Goal?

$$\frac{3}{9} + \frac{5}{30}$$

2. Simplify?

$\frac{3}{9} =$ $\frac{5}{30} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 15 – Level 3

1. Goal?

$$\frac{3}{9} + \frac{5}{30}$$

2. Simplify?

$\frac{3}{9} =$ $\qquad\qquad\qquad$ $\frac{5}{30} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 16 – Solution

1. Goal?

We want to add the fractions $\frac{8}{11}$ and $\frac{4}{12}$.

2. Simplify?

$$\frac{8}{11} \quad ; \quad \frac{4}{12} = \frac{4 \div 4}{12 \div 4} = \frac{1}{3}$$

3. Least Common Denominator

$$\frac{8}{11} = \frac{8 \times 3}{11 \times 3} = \frac{24}{33} \; ; \; \frac{1}{3} = \frac{1 \times 11}{3 \times 11} = \frac{11}{33}$$

4. Add

$$\frac{24}{33} + \frac{11}{33} = \frac{35}{33}$$

5. Simplify?

$\frac{35}{33}$ cannot be simplified.

6. Result

$$\frac{8}{11} + \frac{4}{12} = \frac{8}{11} + \frac{4 \div 4}{12 \div 4} = \frac{8}{11} + \frac{1}{3} = \frac{8 \times 3}{11 \times 3} + \frac{1 \times 11}{3 \times 11} = \frac{24}{33} + \frac{11}{33} = \frac{35}{33}$$

Exercise 16 – Level 1

1. Goal?

$$\frac{8}{11} + \frac{4}{12}$$

2. Simplify?

$$\frac{8}{11} = \qquad\qquad \frac{4}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ |

Exercise 16 – Level 2

1. Goal?

$$\frac{8}{11} + \frac{4}{12}$$

2. Simplify?

$$\frac{8}{11} = \qquad\qquad\qquad \frac{4}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{11}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ |

Exercise 16 – Level 3

1. Goal?

$$\frac{8}{11} + \frac{4}{12}$$

2. Simplify?

$$\frac{8}{11} = \qquad\qquad \frac{4}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 17 – Solution

1. Goal?

We want to add the fractions $\frac{11}{33}$ and $\frac{21}{45}$.

2. Simplify?

$$\frac{11}{33} = \frac{11 \div 11}{33 \div 11} = \frac{1}{3} \quad ; \quad \frac{21}{45} = \frac{21 \div 3}{45 \div 3} = \frac{7}{15}$$

3. Least Common Denominator

$$\frac{1}{3} = \frac{1 \times 5}{3 \times 5} = \frac{5}{15} \ ; \ \frac{7}{15}$$

4. Add

$$\frac{5}{15} + \frac{7}{15} = \frac{12}{15}$$

5. Simplify?

$$\frac{12}{15} = \frac{12 \div 3}{15 \div 3} = \frac{4}{5}$$

6. Result

$$\frac{11}{33}+\frac{21}{45} = \frac{11 \div 11}{33 \div 11}+\frac{21 \div 3}{45 \div 3} = \frac{1}{3}+\frac{7}{15} = \frac{1 \times 5}{3 \times 5}+\frac{7}{15} = \frac{5}{15}+\frac{7}{15} = \frac{12}{15} = \frac{12 \div 3}{15 \div 3} = \frac{4}{5}$$

Exercise 17 – Level 1

1. Goal?

$$\frac{11}{33} + \frac{21}{45}$$

2. Simplify?

$$\frac{11}{33} =$$

$$\frac{21}{45} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 17 – Level 2

---

1. Goal?

$$\frac{11}{33} + \frac{21}{45}$$

---

2. Simplify?

$$\frac{11}{33} = \qquad\qquad\qquad \frac{21}{45} =$$

---

3. Least Common Denominator

---

4. Add

---

5. Simplify?

---

6. Result

Exercise 17 – Level 3

1. Goal?

$$\frac{11}{33} + \frac{21}{45}$$

2. Simplify?

$$\frac{11}{33} = \qquad\qquad \frac{21}{45} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 18 – Solution

1. Goal?

We want to add the fractions $\frac{15}{50}$ and $\frac{7}{35}$.

2. Simplify?

$$\frac{15}{50} = \frac{15 \div 5}{50 \div 5} = \frac{3}{10} \quad ; \quad \frac{7}{35} = \frac{7 \div 7}{35 \div 7} = \frac{1}{5}$$

3. Least Common Denominator

$$\frac{3}{10} \; ; \; \frac{1}{5} = \frac{1 \times 2}{5 \times 2} = \frac{2}{10}$$

4. Add

$$\frac{3}{10} + \frac{2}{10} = \frac{5}{10}$$

5. Simplify?

$$\frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$

6. Result

$$\frac{15}{50} + \frac{7}{35} = \frac{15 \div 5}{50 \div 5} + \frac{7 \div 7}{35 \div 7} = \frac{3}{10} + \frac{1}{5} = \frac{3}{10} + \frac{1 \times 2}{5 \times 2} = \frac{3}{10} + \frac{2}{10} = \frac{5}{10} = \frac{5 \div 5}{10 \div 5} = \frac{1}{2}$$

Exercise 18 – Level 1

1. Goal?

$$\frac{15}{50} + \frac{7}{35}$$

2. Simplify?

$$\frac{15}{50} = \qquad\qquad \frac{7}{35} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 18 – Level 2

1. Goal?

$$\frac{15}{50} + \frac{7}{35}$$

2. Simplify?

$$\frac{15}{50} = \qquad\qquad \frac{7}{35} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 18 – Level 3

1. Goal?

$$\frac{15}{50} + \frac{7}{35}$$

2. Simplify?

$$\frac{15}{50} =$$

$$\frac{7}{35} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

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Exercise 19 – Solution

1. Goal?

We want to add the fractions $\frac{8}{12}$ and $\frac{4}{21}$.

2. Simplify?

$$\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3} \quad ; \quad \frac{4}{21}$$

3. Least Common Denominator

$$\frac{2}{3} = \frac{2 \times 7}{3 \times 7} = \frac{14}{21} \; ; \; \frac{4}{21}$$

4. Add

$$\frac{14}{21} + \frac{4}{21} = \frac{18}{21}$$

5. Simplify?

$$\frac{18}{21} = \frac{18 \div 3}{21 \div 3} = \frac{6}{7}$$

6. Result

$$\frac{8}{12} + \frac{4}{21} = \frac{8 \div 4}{12 \div 4} + \frac{4}{21} = \frac{2}{3} + \frac{4}{21} = \frac{2 \times 7}{3 \times 7} + \frac{4}{21} = \frac{14}{21} + \frac{4}{21} = \frac{18}{21} = \frac{18 \div 3}{21 \div 3} = \frac{6}{7}$$

Exercise 19 – Level 1

1. Goal?

$$\frac{8}{12} + \frac{4}{21}$$

2. Simplify?

$$\frac{8}{12} =$$
$$\frac{4}{21} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 19 – Level 2

1. Goal?

$$\frac{8}{12} + \frac{4}{21}$$

2. Simplify?

$$\frac{8}{12} = \qquad\qquad \frac{4}{21} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ |

Exercise 19 – Level 3

1. Goal?

$$\frac{8}{12} + \frac{4}{21}$$

2. Simplify?

$$\frac{8}{12} = \qquad\qquad \frac{4}{21} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 20 – Solution

1. Goal?

We want to add the fractions $\frac{10}{16}$ and $\frac{4}{20}$.

2. Simplify?

$$\frac{10}{16} = \frac{10 \div 2}{16 \div 2} = \frac{5}{8} \quad ; \quad \frac{4}{20} = \frac{4 \div 4}{20 \div 4} = \frac{1}{5}$$

3. Least Common Denominator

$$\frac{5}{8} = \frac{5 \times 5}{8 \times 5} = \frac{25}{40} \ ; \ \frac{1}{5} = \frac{1 \times 8}{5 \times 8} = \frac{8}{40}$$

4. Add

$$\frac{25}{40} + \frac{8}{40} = \frac{33}{40}$$

5. Simplify?

$\frac{33}{40}$ cannot be simplified.

6. Result

$$\frac{10}{16} + \frac{4}{20} = \frac{10 \div 2}{16 \div 2} + \frac{4 \div 4}{20 \div 4} = \frac{5}{8} + \frac{1}{5} = \frac{5 \times 5}{8 \times 5} + \frac{1 \times 8}{5 \times 8} = \frac{25}{40} + \frac{8}{40} = \frac{33}{40}$$

Exercise 20 – Level 1

1. Goal?

$$\frac{10}{16} + \frac{4}{20}$$

2. Simplify?

$$\frac{10}{16} = \qquad\qquad \frac{4}{20} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ | $\frac{1}{20}$ |

Exercise 20 – Level 2

1. Goal?

$$\frac{10}{16} + \frac{4}{20}$$

2. Simplify?

$$\frac{10}{16} =$$ $$\frac{4}{20} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 20 – Level 3

1. Goal?

$$\frac{10}{16} + \frac{4}{20}$$

2. Simplify?

$\frac{10}{16} =$ $\qquad\qquad\qquad\qquad\qquad$ $\frac{4}{20} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 21 – Solution

1. Goal?

We want to add the fractions $\frac{24}{45}$ and $\frac{6}{36}$.

2. Simplify?

$$\frac{24}{45} = \frac{24 \div 3}{45 \div 3} = \frac{8}{15} \quad ; \quad \frac{6}{36} = \frac{6 \div 6}{36 \div 6} = \frac{1}{6}$$

3. Least Common Denominator

$$\frac{8}{15} = \frac{8 \times 2}{15 \times 2} = \frac{16}{30} \; ; \; \frac{1}{6} = \frac{1 \times 5}{6 \times 5} = \frac{5}{30}$$

4. Add

$$\frac{16}{30} + \frac{5}{30} = \frac{21}{30}$$

5. Simplify?

$$\frac{21}{30} = \frac{21 \div 3}{30 \div 3} = \frac{7}{10}$$

6. Result

$$\frac{24}{45}+\frac{6}{36} = \frac{24 \div 3}{45 \div 3}+\frac{6 \div 6}{36 \div 6} = \frac{8}{15}+\frac{1}{6} = \frac{8 \times 2}{15 \times 2}+\frac{1 \times 5}{6 \times 5} = \frac{16}{30}+\frac{5}{30} = \frac{21}{30} = \frac{21 \div 3}{30 \div 3} = \frac{7}{10}$$

Exercise 21 – Level 1

1. Goal?

$$\frac{24}{45} + \frac{6}{36}$$

2. Simplify?

$$\frac{24}{45} = \qquad\qquad \frac{6}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 21 – Level 2

1. Goal?

$$\frac{24}{45} + \frac{6}{36}$$

2. Simplify?

$$\frac{24}{45} = \qquad\qquad \frac{6}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 21 – Level 3

1. Goal?

$$\frac{24}{45} + \frac{6}{36}$$

2. Simplify?

$$\frac{24}{45} =$$
$$\frac{6}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 22 – Solution

1. Goal?

We want to add the fractions $\frac{35}{42}$ and $\frac{15}{54}$.

2. Simplify?

$$\frac{35}{42} = \frac{35 \div 7}{42 \div 7} = \frac{5}{6} \quad ; \quad \frac{15}{54} = \frac{15 \div 3}{54 \div 3} = \frac{5}{18}$$

3. Least Common Denominator

$$\frac{5}{6} = \frac{5 \times 3}{6 \times 3} = \frac{15}{18} \; ; \; \frac{5}{18}$$

4. Add

$$\frac{15}{18} + \frac{5}{18} = \frac{20}{18}$$

5. Simplify?

$$\frac{20}{18} = \frac{20 \div 2}{18 \div 2} = \frac{10}{9}$$

6. Result

$$\frac{35}{42}+\frac{15}{54} = \frac{35 \div 7}{42 \div 7}+\frac{15 \div 3}{54 \div 3} = \frac{5}{6}+\frac{5}{18} = \frac{5 \times 3}{6 \times 3}+\frac{5}{18} = \frac{15}{18}+\frac{5}{18} = \frac{20}{18} = \frac{20 \div 2}{18 \div 2} = \frac{10}{9}$$

Exercise 22 – Level 1

1. Goal?

$$\frac{35}{42} + \frac{15}{54}$$

2. Simplify?

$$\frac{35}{42} =$$

$$\frac{15}{54} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 22 – Level 2

1. Goal?

$$\frac{35}{42} + \frac{15}{54}$$

2. Simplify?

$$\frac{35}{42} = \qquad\qquad \frac{15}{54} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 22 – Level 3

1. Goal?

$$\frac{35}{42} + \frac{15}{54}$$

2. Simplify?

$\frac{35}{42} =$ $\frac{15}{54} =$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 23 – Level 1

1. Goal?

$$\frac{10}{12} + \frac{4}{40}$$

2. Simplify?

$$\frac{10}{12} =$$ $$\frac{4}{40} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{40}$ | $\frac{1}{40}$ | $\frac{1}{40}$ | $\frac{1}{40}$ |

Exercise 23 – Level 2

1. Goal?

$$\frac{10}{12} + \frac{4}{40}$$

2. Simplify?

$$\frac{10}{12} =$$ $$\frac{4}{40} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{12}$ | $\frac{1}{40}$ | $\frac{1}{40}$ | $\frac{1}{40}$ | $\frac{1}{40}$ |

Exercise 23 – Level 3

1. Goal?

$$\frac{10}{12} + \frac{4}{40}$$

2. Simplify?

$$\frac{10}{12} =$$

$$\frac{4}{40} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 24 – Solution

1. Goal?

We want to add the fractions $\frac{10}{24}$ and $\frac{9}{36}$.

2. Simplify?

$$\frac{10}{24} = \frac{10 \div 2}{24 \div 2} = \frac{5}{12} \qquad \frac{9}{36} = \frac{9 \div 9}{36 \div 9} = \frac{1}{4}$$

3. Least Common Denominator

$$\frac{5}{12} \ ; \ \frac{1}{4} = \frac{1 \times 3}{4 \times 3} = \frac{3}{12}$$

4. Add

$$\frac{5}{12} + \frac{3}{12} = \frac{8}{12}$$

5. Simplify?

$$\frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

6. Result

$$\frac{10}{24} + \frac{9}{36} = \frac{10 \div 2}{24 \div 2} + \frac{9 \div 9}{36 \div 9} = \frac{5}{12} + \frac{1}{4} = \frac{5}{12} + \frac{1 \times 3}{4 \times 3} = \frac{5}{12} + \frac{3}{12} = \frac{8}{12} = \frac{8 \div 4}{12 \div 4} = \frac{2}{3}$$

Exercise 24 – Level 1

1. Goal?

$$\frac{10}{24} + \frac{9}{36}$$

2. Simplify?

$$\frac{10}{24} = \qquad\qquad\qquad \frac{9}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 24 – Level 2

1. Goal?

$$\frac{10}{24} + \frac{9}{36}$$

2. Simplify?

$$\frac{10}{24} = \qquad\qquad\qquad \frac{9}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

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Exercise 24 – Level 3

1. Goal?

$$\frac{10}{24} + \frac{9}{36}$$

2. Simplify?

$$\frac{10}{24} =$$

$$\frac{9}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 25 – Solution

1. Goal?

We want to add the fractions $\frac{9}{21}$ and $\frac{8}{32}$.

2. Simplify?

$$\frac{9}{21} = \frac{9 \div 3}{21 \div 3} = \frac{3}{7} \quad ; \quad \frac{8}{32} = \frac{8 \div 8}{32 \div 8} = \frac{1}{4}$$

3. Least Common Denominator

$$\frac{3}{7} = \frac{3 \times 4}{7 \times 4} = \frac{12}{28} \ ; \ \frac{1}{4} = \frac{1 \times 7}{4 \times 7} = \frac{7}{28}$$

4. Add

$$\frac{12}{28} + \frac{7}{28} = \frac{19}{28}$$

5. Simplify?

$\frac{19}{28}$ cannot be simplified.

6. Result

$$\frac{9}{21} + \frac{8}{32} = \frac{3 \div 3}{21 \div 3} + \frac{8 \div 8}{32 \div 8} = \frac{3}{7} + \frac{1}{4} = \frac{3 \times 4}{7 \times 4} + \frac{1 \times 7}{4 \times 7} = \frac{12}{28} + \frac{7}{28} = \frac{19}{28}$$

Exercise 25 – Level 1

1. Goal?

$$\frac{9}{21} + \frac{8}{32}$$

2. Simplify?

$$\frac{9}{21} = \qquad\qquad\qquad \frac{8}{32} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ | $\frac{1}{32}$ |

Exercise 25 – Level 2

1. Goal?

$$\frac{9}{21} + \frac{8}{32}$$

2. Simplify?

$$\frac{9}{21} =$$

$$\frac{8}{32} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 25 – Level 3

1. Goal?

$$\frac{9}{21} + \frac{8}{32}$$

2. Simplify?

$$\frac{9}{21} = \qquad\qquad \frac{8}{32} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 26 – Solution

1. Goal?

We want to add the fractions $\frac{9}{24}$ and $\frac{15}{27}$.

2. Simplify?

$$\frac{9}{24} = \frac{9 \div 3}{24 \div 3} = \frac{3}{8} \quad ; \quad \frac{15}{27} = \frac{15 \div 3}{27 \div 3} = \frac{5}{9}$$

3. Least Common Denominator

$$\frac{3}{8} = \frac{3 \times 9}{8 \times 9} = \frac{27}{72} \; ; \; \frac{5}{9} = \frac{5 \times 8}{9 \times 8} = \frac{40}{72}$$

4. Add

$$\frac{27}{72} + \frac{40}{72} = \frac{67}{72}$$

5. Simplify?

$\frac{67}{72}$ cannot be simplified.

6. Result

$$\frac{9}{24} + \frac{15}{27} = \frac{9 \div 3}{24 \div 3} + \frac{15 \div 3}{27 \div 3} = \frac{3}{8} + \frac{5}{9} = \frac{3 \times 9}{8 \times 9} + \frac{5 \times 8}{9 \times 8} = \frac{27}{72} + \frac{40}{72} = \frac{67}{72}$$

Exercise 26 – Level 1

1. Goal?

$$\frac{9}{24} + \frac{15}{27}$$

2. Simplify?

$$\frac{9}{24} = \qquad\qquad \frac{15}{27} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 26 – Level 2

1. Goal?

$$\frac{9}{24} + \frac{15}{27}$$

2. Simplify?

$$\frac{9}{24} =$$ $$\frac{15}{27} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{24}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ | $\frac{1}{27}$ |

Exercise 26 – Level 3

1. Goal?

$$\frac{9}{24} + \frac{15}{27}$$

2. Simplify?

$$\frac{9}{24} =$$

$$\frac{15}{27} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 27 – Solution

1. Goal?

We want to add the fractions $\frac{21}{56}$ and $\frac{10}{16}$.

2. Simplify?

$\frac{21}{56} = \frac{21 \div 7}{56 \div 7} = \frac{3}{8}$ and $\frac{10}{16} = \frac{10 \div 2}{16 \div 2} = \frac{5}{8}$

3. Least Common Denominator

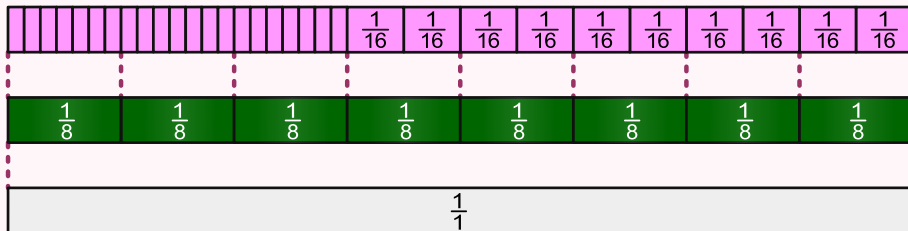$$\frac{3}{8} \; ; \; \frac{5}{8}$$

4. Add

$$\frac{3}{8} + \frac{5}{8} = \frac{8}{8}$$

5. Simplify?

$$\frac{8}{8} = \frac{8 \div 8}{8 \div 8} = \frac{1}{1} = 1$$

6. Result

$$\frac{21}{56} + \frac{10}{16} = \frac{21 \div 7}{56 \div 7} + \frac{10 \div 2}{16 \div 2} = \frac{3}{8} + \frac{5}{8} = \frac{8}{8} = \frac{8 \div 8}{8 \div 8} = \frac{1}{1} = 1$$

Exercise 27 – Level 1

1. Goal?
$$\frac{21}{56} + \frac{10}{16}$$

2. Simplify?

$$\frac{21}{56} =$$
$$\frac{10}{16} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ |

Exercise 27 – Level 2

1. Goal?

$$\frac{21}{56} + \frac{10}{16}$$

2. Simplify?

$$\frac{21}{56} = \qquad\qquad \frac{10}{16} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ | $\frac{1}{16}$ |

Exercise 27 – Level 3

1. Goal?

$$\frac{21}{56} + \frac{10}{16}$$

2. Simplify?

$$\frac{21}{56} =$$
$$\frac{10}{16} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 28 – Solution

1. Goal? We want to add the fractions $\frac{6}{21}$ and $\frac{6}{28}$.

2. Simplify? $\frac{6}{21} = \frac{6 \div 3}{21 \div 3} = \frac{2}{7}$ and $\frac{6}{28} = \frac{6 \div 2}{28 \div 2} = \frac{3}{14}$

3. Least Common Denominator
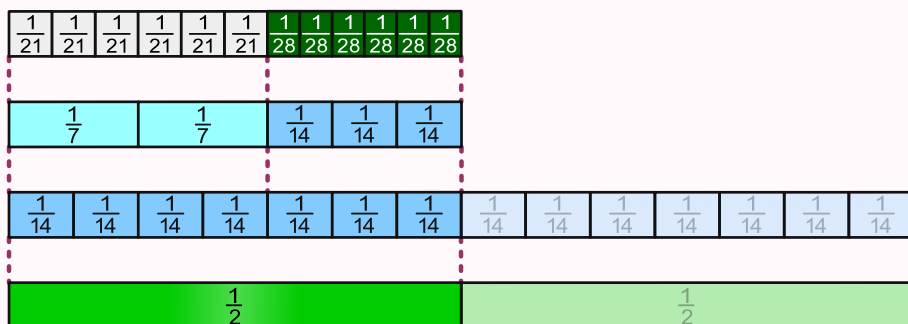$$\frac{2}{7} = \frac{2 \times 2}{7 \times 2} = \frac{4}{14} \; ; \quad \frac{3}{14}$$

4. Add
$$\frac{4}{14} + \frac{3}{14} = \frac{7}{14}$$

5. Simplify?
$$\frac{7}{14} = \frac{7 \div 7}{14 \div 7} = \frac{1}{2}$$

6. Result

$$\frac{6}{21} + \frac{6}{28} = \frac{6 \div 3}{21 \div 3} + \frac{6 \div 2}{28 \div 2} = \frac{2}{7} + \frac{3}{14} = \frac{2 \times 2}{7 \times 2} + \frac{3}{14} = \frac{4}{14} + \frac{3}{14} = \frac{7}{14} = \frac{7 \div 7}{14 \div 7} = \frac{1}{2}$$

Exercise 28 – Level 1

1. Goal?

$$\frac{6}{21} + \frac{6}{28}$$

2. Simplify?

$$\frac{6}{21} =$$
$$\frac{6}{28} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ |

Exercise 28 – Level 2

1. Goal?

$$\frac{6}{21} + \frac{6}{28}$$

2. Simplify?

$$\frac{6}{21} = \qquad\qquad \frac{6}{28} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$\frac{1}{21}$ $\frac{1}{21}$ $\frac{1}{21}$ $\frac{1}{21}$ $\frac{1}{21}$ $\frac{1}{21}$ $\frac{1}{28}$ $\frac{1}{28}$ $\frac{1}{28}$ $\frac{1}{28}$ $\frac{1}{28}$ $\frac{1}{28}$

Exercise 28 – Level 3

1. Goal?

$$\frac{6}{21} + \frac{6}{28}$$

2. Simplify?

$$\frac{6}{21} =$$

$$\frac{6}{28} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

| $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{21}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ | $\frac{1}{28}$ |

Exercise 29 – Solution

1. Goal? We want to add the fractions $\frac{12}{45}$ and $\frac{10}{12}$.

2. Simplify? $\frac{12}{45} = \frac{12 \div 3}{45 \div 3} = \frac{4}{15}$ and $\frac{10}{12} = \frac{10 \div 2}{12 \div 2} = \frac{5}{6}$

3. Least Common Denominator

$$\frac{4}{15} = \frac{4 \times 2}{15 \times 2} = \frac{8}{30} \; ; \; \frac{5}{6} = \frac{5 \times 5}{6 \times 5} = \frac{25}{30}$$

4. Add

$$\frac{8}{30} + \frac{25}{30} = \frac{33}{30}$$

5. Simplify?

$$\frac{33}{30} = \frac{33 \div 3}{30 \div 3} = \frac{11}{10}$$

6. Result

$$\frac{12}{45} + \frac{10}{12} = \frac{12 \div 3}{45 \div 3} + \frac{10 \div 2}{12 \div 2} = \frac{4}{15} + \frac{5}{6} = \frac{4 \times 2}{15 \times 2} + \frac{5 \times 5}{6 \times 5} = \frac{8}{30} + \frac{25}{30} = \frac{33}{30} = \frac{33 \div 3}{30 \div 3} = \frac{11}{10}$$

Exercise 29 – Level 1

1. Goal?

$$\frac{12}{45} + \frac{10}{12}$$

2. Simplify?

$$\frac{12}{45} =$$

$$\frac{10}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 29 – Level 2

1. Goal?

$$\frac{12}{45} + \frac{10}{12}$$

2. Simplify?

$$\frac{12}{45} =$$
$$\frac{10}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 29 – Level 3

1. Goal?

$$\frac{12}{45} + \frac{10}{12}$$

2. Simplify?

$$\frac{12}{45} = \qquad\qquad \frac{10}{12} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 30 – Solution

1. Goal?

We want to add the fractions $\frac{6}{27}$ and $\frac{1}{36}$.

2. Simplify?

$$\frac{6}{27} = \frac{6 \div 3}{27 \div 3} = \frac{2}{9} \text{ and } \frac{1}{36}$$

3. Least Common Denominator

$$\frac{2}{9} = \frac{2 \times 4}{9 \times 4} = \frac{8}{36} \; ; \quad \frac{1}{36}$$
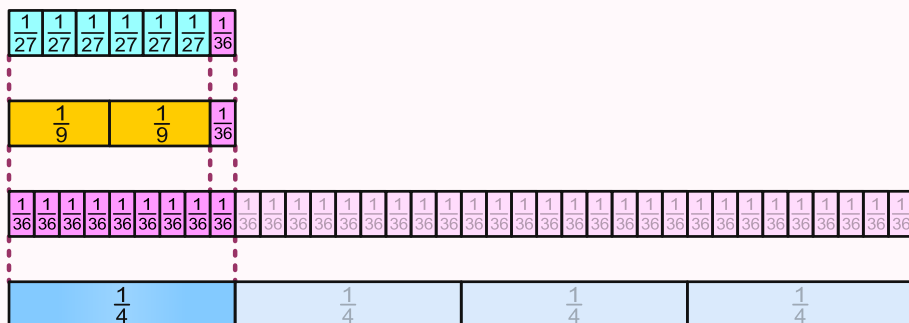
4. Add

$$\frac{8}{36} + \frac{1}{36} = \frac{9}{36}$$

5. Simplify?

$$\frac{9}{36} = \frac{9 \div 9}{36 \div 9} = \frac{1}{4}$$

6. Result

$$\frac{6}{27} + \frac{1}{36} = \frac{6 \div 3}{27 \div 3} + \frac{1}{36} = \frac{2}{9} + \frac{1}{36} = \frac{2 \times 4}{9 \times 4} + \frac{1}{36} = \frac{8}{36} + \frac{1}{36} = \frac{9}{36} = \frac{9 \div 9}{36 \div 9} = \frac{1}{4}$$

Exercise 30 – Level 1

1. Goal?

$$\frac{6}{27} + \frac{1}{36}$$

2. Simplify?

$$\frac{6}{27} =$$

$$\frac{1}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 30 – Level 2

1. Goal?

$$\frac{6}{27} + \frac{1}{36}$$

2. Simplify?

$$\frac{6}{27} = \qquad\qquad \frac{1}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$$\frac{1}{27}\;\frac{1}{27}\;\frac{1}{27}\;\frac{1}{27}\;\frac{1}{27}\;\frac{1}{27}\;\frac{1}{36}$$

Exercise 30 – Level 3

1. Goal?

$$\frac{6}{27} + \frac{1}{36}$$

2. Simplify?

$$\frac{6}{27} = \qquad\qquad \frac{1}{36} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

$$\frac{1}{27}\ \frac{1}{27}\ \frac{1}{27}\ \frac{1}{27}\ \frac{1}{27}\ \frac{1}{27}\ \frac{1}{36}$$

Exercise 31 – Solution

1. Goal?

We want to add the fractions $\frac{6}{105}$ and $\frac{27}{42}$.

2. Simplify?

$\frac{6}{105} = \frac{6 \div 3}{105 \div 3} = \frac{2}{35}$ and $\frac{27}{42} = \frac{27 \div 3}{42 \div 3} = \frac{9}{14}$

3. Least Common Denominator

$$\frac{2}{35} = \frac{2 \times 2}{35 \times 2} = \frac{4}{70} \ ; \ \ \frac{9}{14} = \frac{9 \times 5}{14 \times 5} = \frac{45}{70}$$

4. Add

$$\frac{4}{70} + \frac{45}{70} = \frac{49}{70}$$

5. Simplify?

$$\frac{49}{70} = \frac{49 \div 7}{70 \div 7} = \frac{7}{10}$$

6. Result

$$\frac{6}{105} + \frac{27}{42} = \frac{6 \div 3}{105 \div 3} + \frac{27 \div 3}{42 \div 3} = \frac{2}{35} + \frac{9}{14} = \frac{2 \times 2}{35 \times 2} + \frac{9 \times 5}{14 \times 5} = \frac{4}{70} + \frac{45}{70} = \frac{49}{70} = \frac{49 \div 7}{70 \div 7} = \frac{7}{10}$$

Exercise 31 – Level 1

1. Goal?
$$\frac{6}{105} + \frac{27}{42}$$

2. Simplify?

$$\frac{6}{105} =$$
$$\frac{27}{42} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 31 – Level 2

1. Goal?

$$\frac{6}{105} + \frac{27}{42}$$

2. Simplify?

$$\frac{6}{105} = \qquad\qquad \frac{27}{42} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 31 – Level 3

1. Goal?

$$\frac{6}{105} + \frac{27}{42}$$

2. Simplify?

$$\frac{6}{105} =$$

$$\frac{27}{42} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 32 – Solution

1. Goal?

We want to add the fractions $\frac{8}{42}$ and $\frac{26}{39}$.

2. Simplify? $\frac{8}{42} = \frac{8 \div 2}{42 \div 2} = \frac{4}{21}$ and $\frac{26}{39} = \frac{26 \div 13}{39 \div 13} = \frac{2}{3}$

3. Least Common Denominator
$$\frac{4}{21} \; ; \quad \frac{2}{3} = \frac{2 \times 7}{3 \times 7} = \frac{14}{21}$$

4. Add
$$\frac{4}{21} + \frac{14}{21} = \frac{18}{21}$$

5. Simplify?
$$\frac{18}{21} = \frac{18 \div 3}{21 \div 3} = \frac{6}{7}$$

6. Result

$$\frac{8}{42} + \frac{26}{39} = \frac{8 \div 2}{42 \div 2} + \frac{26 \div 13}{39 \div 13} = \frac{4}{21} + \frac{2}{3} = \frac{4}{21} + \frac{2 \times 7}{3 \times 7} = \frac{4}{21} + \frac{14}{21} = \frac{18}{21} = \frac{18 \div 3}{21 \div 3} = \frac{6}{7}$$

Exercise 32 – Level 1

1. Goal?

$$\frac{8}{42} + \frac{26}{39}$$

2. Simplify?

$$\frac{8}{42} = \qquad\qquad \frac{26}{39} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 32 – Level 2

1. Goal?

$$\frac{8}{42} + \frac{26}{39}$$

2. Simplify?

$$\frac{8}{42} =$$

$$\frac{26}{39} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result

Exercise 32 – Level 3

1. Goal?

$$\frac{8}{42} + \frac{26}{39}$$

2. Simplify?

$$\frac{8}{42} =$$ 　　　　　　　　 $$\frac{26}{39} =$$

3. Least Common Denominator

4. Add

5. Simplify?

6. Result